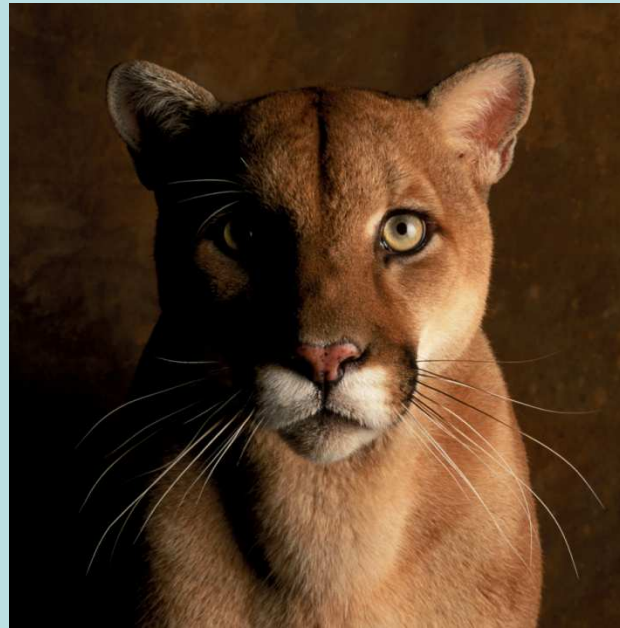
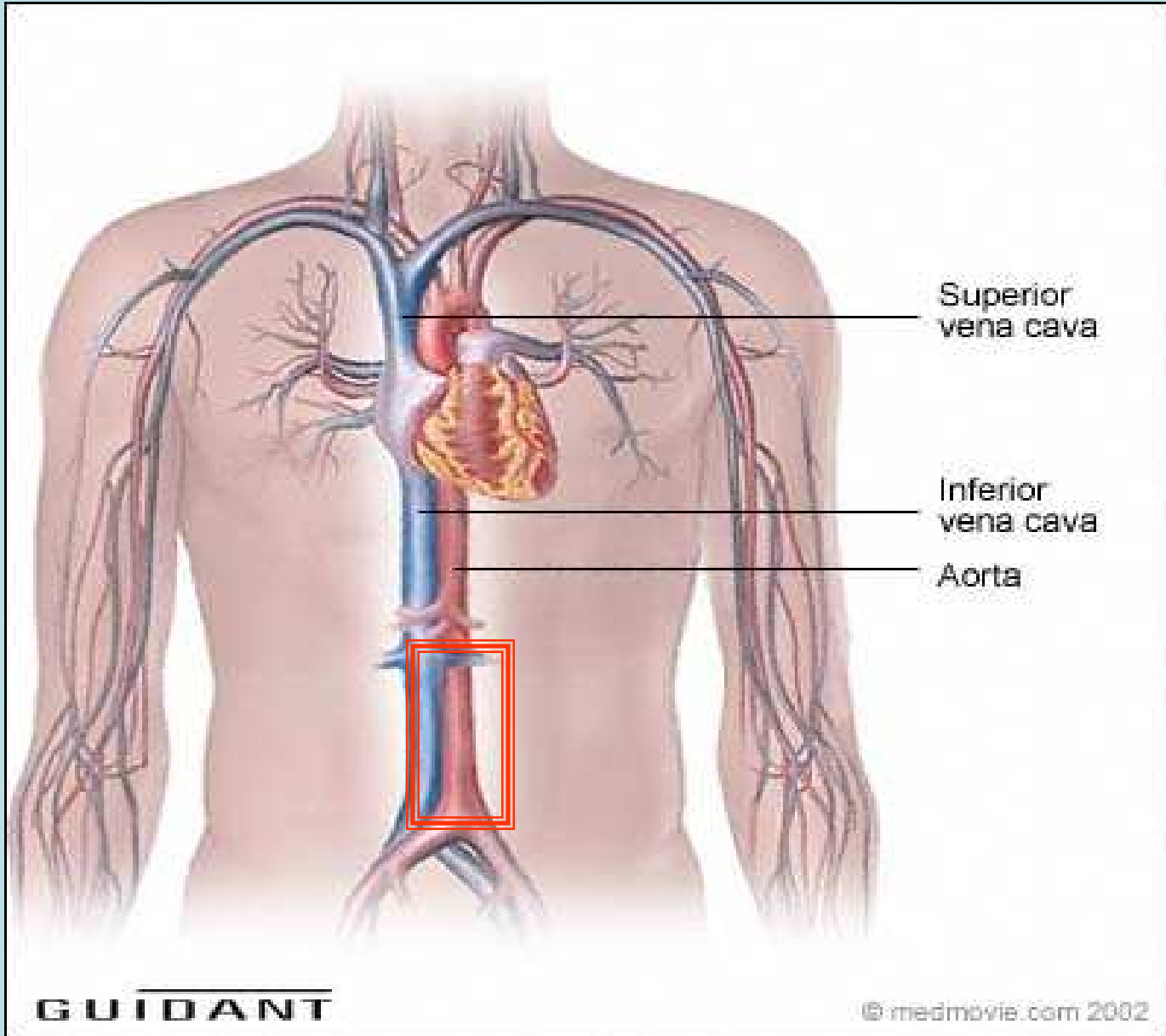


# MATHEMATICS AND CARDIOLOGY: PARTNERS FOR THE FUTURE



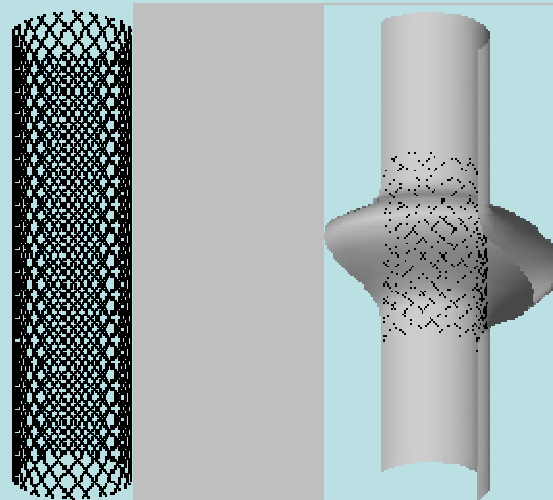
**Suncica Canic**  
Department of Mathematics  
University of Houston





**Aneurysm is characterized by the formation of sac-like protrusions of weakened sections of blood vessels that can rupture and be fatal. There is a 90% mortality rate associated with an out-of-hospital AAA rupture. Until recently, surgery has been the only treatment to prevent the aneurysm from rupturing. Since most of the patients are 55 or older and high risk, undergoing general anesthesia is not a solution.**

**Within the past ten years an innovative non-invasive procedure, which requires only local anesthesia, has been developed. The new procedure entails inserting a catheter into an artery and directing it to the site of the aneurysm. Placed in the catheter is a spring-like device called a stent, which serves to hold open the weakened artery and to exclude the aneurysm from circulation. This lowers the probability of rupture and promotes aneurysm shrinking due to thrombosis caused by the lack of blood supply to the aneurysm tissue.**



**The procedure is still considered experimental and reports of mid- or long-term outcomes indicate structural and positional changes of the stent, including buckling, kinking and migration. To improve the procedure, optimal stent design depending on the patient's anatomy and a study of the optimal anchoring strategies are needed.**

**e.**

# PROBLEM

## FLUID-STRUCTURE INTERACTION BETWEEN BLOOD FLOW AND ARTERIAL WALLS IN HEALTHY AND DISEASED STATES

### ANALYSIS OF FLUID-STRUCTURE INTERACTION CAN:

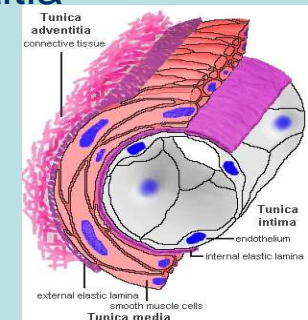
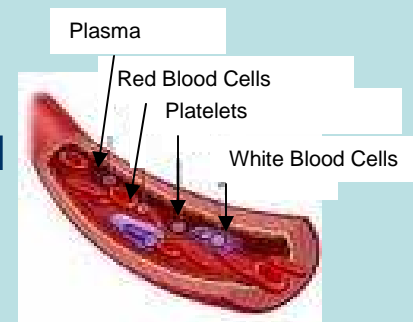
1. Help predict initiation of disease
2. Help improve treatment of disease

- aortic abdominal aneurysm (AAA) repair
- coronary artery disease (CAD) repair.

Prostheses design  
for non-surgical treatment  
of AAA and CAD

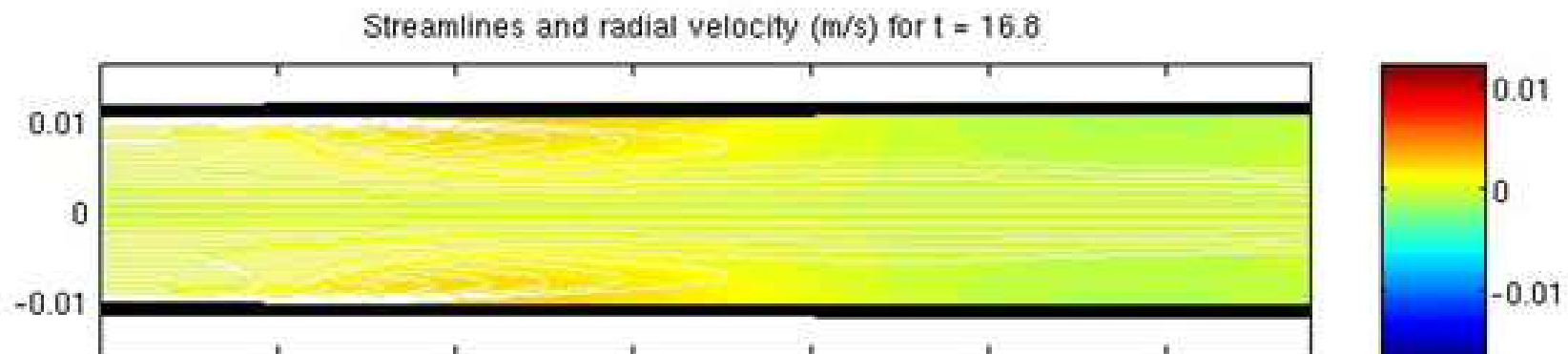
# DIFFICULT PROBLEM TO STUDY: MULTI-PHYSICS AND MULTI-SCALE NATURE

- BLOOD has complicated rheology: red blood cells, white blood cells and platelets in plasma (relevant at small scales)
- VESSEL WALLS have complex structure: intima, media, adventitia (+ smaller scales layers); different mech. char.
- Challenging to model.
- INTERACTION (COUPLING) exceedingly complicated.



# COUPLING BETWEEN BLOOD FLOW AND VESSEL WALL MOTION

- **NONLINEAR COUPLING:** density of the arterial walls is roughly the same as density of blood
  - algorithms developed for other applications, e.g. aeroelasticity, UNSTABLE;
    - novel ideas and algorithms needed
- **TWO TIME SCALES:** fast traveling waves in arterial walls and slow bulk blood flow velocity
  - resolving both scales accurately requires sophisticated methods
- **COMPETITION BETWEEN “HYPERBOLIC” AND “PARABOLIC” EFFECTS** (wave propagation vs. diffusion)
  - resolving the two different effects requires different techniques



# COMPREHENSIVE STUDY OF FLUID-STRUCTURE INTERACTION IN BLOOD FLOW

(medium-to-large arteries: laminar flow and  $Re$  away from the turbulent regime)

## ANALYSIS

- Fundamental properties of the interaction and of the solution.
- Derivation of new closed, effective models.



## COMPUTATION

- Design of a numerical algorithm (“kinematically coupled”) with a novel operator splitting approach (hyperbolic/parabolic) with improved stability properties.
- Models allowing two different structures (stent modeling).
- Fluid-cell-structure interaction algorithm

## VALIDATION AND TREATMENT

- Experimental validation.
- Application to AAA repair and coronary angioplasty with stenting

TEXAS  
MEDICAL  
CENTER  
HOUSTON

# STUDY OPTIMAL PROSTHESIS DESIGN FOR AAA REPAIR

## METHODS

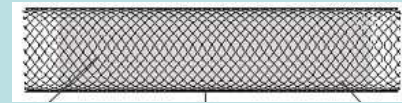
- EXPERIMENTAL MEASUREMENTS OF PROSTHESES MECHANICAL PROPERTIES (Ravi-Chandar, UT Austin)
- MATHEMATICAL MODELING OF PROSTHESES MECHANICS AND DYNAMICS
- COMPUTER SIMULATIONS
- EXPERIMENTAL VALIDATION



# RESULTS LEAD TO NEW STENT-GRAFT DESIGN

## MODELING AND COMPUTATION PRODUCED:

### •RESULTS FOR FLEXIBLE bare Wallstent.



- Wallstent 10 times more elastic than aorta: large radial displacements [ANGIO](#)
- large stresses and strains near anchoring (possibility of migration) [PLAY MOVIE](#) Next slide →

POOR PERFORMANCE → NO LONGER USED

### •RESULTS FOR FABRIC-COVERED STENT-GRAFTS

- graft is stiff; elastic exoskeleton tends to pulsate: possibility for suture breakage
- stiff graft: elevated local transmural pressure [COMPARISON MOVIE](#)



→ NON-UNIFORM STIFNESS MINIMIZES STRESS AT ANCHORING

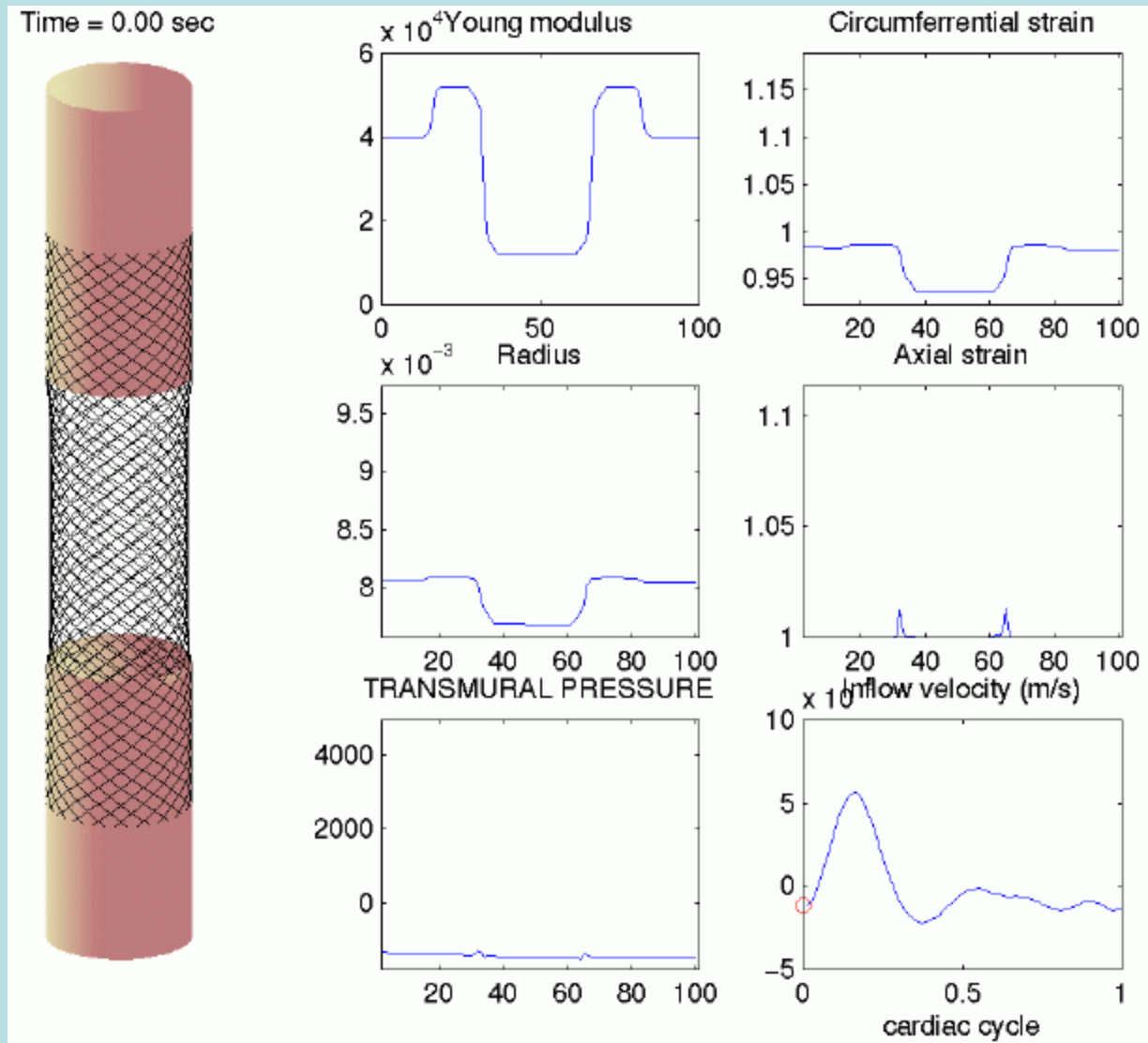
[1] Canic, Krajcer, Lapin, Endovascular Today (2006)

[2] Canic, Krajcer, Chandar, Mirkovic, Lapin, Texas Heart Institute Journal (2005)

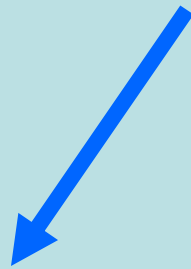
[3] R. Wang and K. Ravi-Chandar, Mechanical response of an aortic stent I and II *Journal of Appl. Mechanics*, (2004.)

[4] SIAM News, Vol. 37 No. 4 (2004) Dana McKennzie

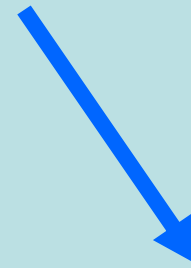
# AAA Walstent (compliant)



# MATHEMATICAL MODELING AND COMPUTATION



**DETECT DEVICE'S  
STRUCTURAL DEFICIENCIES**



**SUGGEST IMPROVED  
DEVICE DESIGN**

# MATHEMATICAL PROBLEM

## FLUID-CELL-STRUCTURE INTERACTION

### FLUID (BLOOD)

Newtonian, incompressible  
fluid

Unsteady

Incompressible Navier-Stokes

### COMPLIANT WALLS

[SIAP '06, SIAMMS '05, Annals of Bimed Eng '05, CRAS '04, SIADS '03, CRAS '02]

Linearly ELASTIC and linearly VISCOELASTIC

Koiter SHELL model (Koiter, Ciarlet et al.)

Linearly ELASTIC and linearly VISCOELASTIC MEMBRANE model

NONLINEARLY ELASTIC MEMBRANE

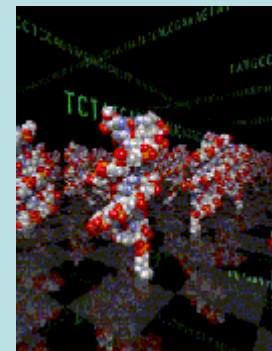
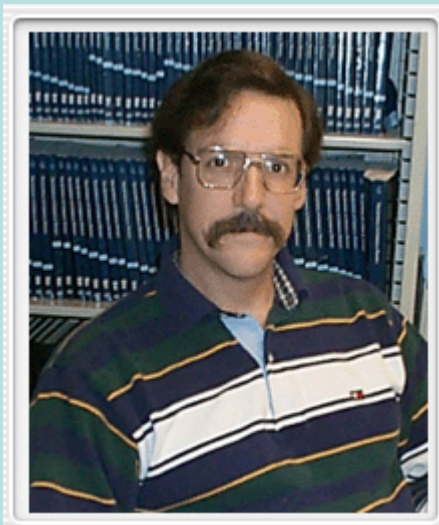
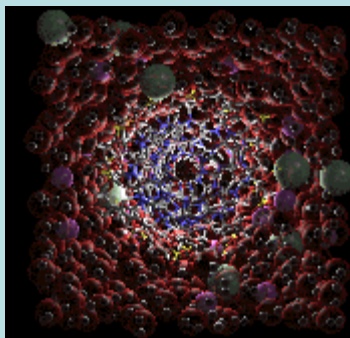
### CELLS

Auricular chondrocytes

Cell adhesion and detachment

Hammer's adhesion dynamics algorithm

**MATHEMATICAL FLUID-STRUCTURE  
INTERACTION IN BLOOD FLOW**



**B. Montgomery Pettitt**

**Hugh Roy and Lille Cranz Cullen Distinguished Professor of  
Chemistry, Physics, Computer Science, Biology and Biochemistry,**

**Director of the Institute for Molecular Design**

.

**Effects of anisotropic environments on DNA and Proteins**

**Computational methods to investigate solution systems with couplings and correlations at many disparate length and time scales**

**Simulation of fundamental structure and dynamics of the liquid state: Most difficult is the question of ions in aqueous solution and biomolecular solutions**

**Computational methods to explore phase transitions in saline solution and protein folding in multicomponent systems.**



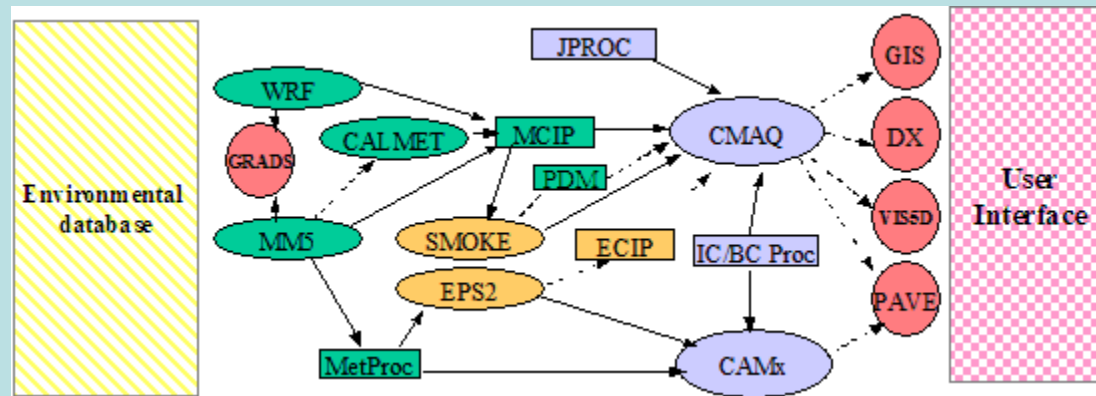


**Air Quality Modeling**  
**Dr. Daewon Byun**  
**Director, Institute for Multi Dimensional Air Quality Studies**

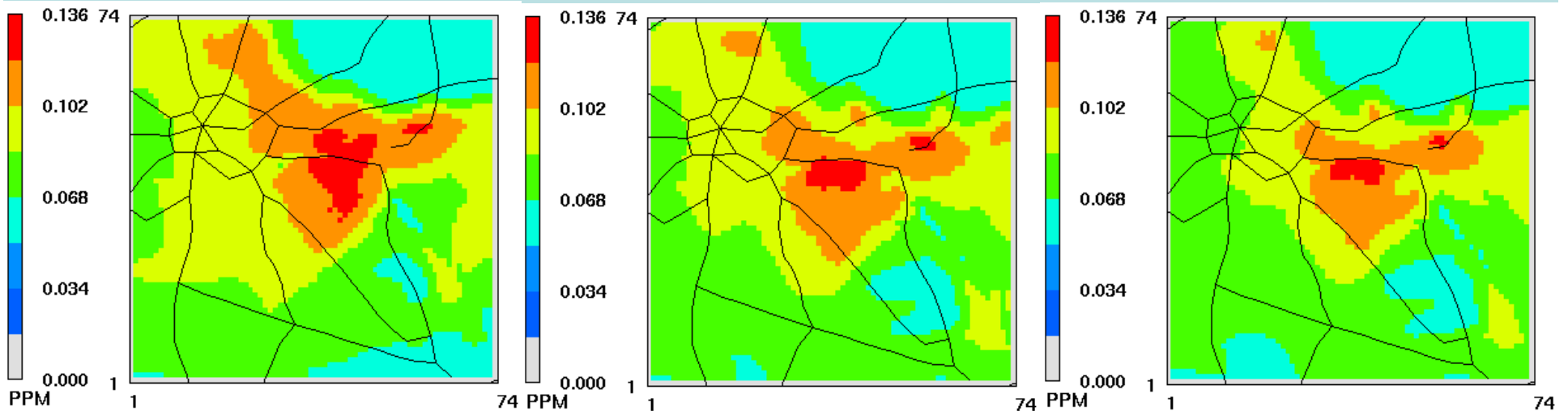


The modeling paradigm that incorporates different meteorological models, two emission inventory models, and two chemical transport models were used, along with assorted supporting pre- and inter-processing programs. The primary analysis tools are based on the Community Multiscale Air Quality (CMAQ) modeling system which is the latest Eulerian air quality model made available by the U.S. EPA. CMAQ employs the best available techniques for advection, diffusion, and complex chemical transformation of a variety of pollutants. The system consists of three primary components (meteorology, emissions, and a chemical transport model) and several interface processors.

The arrows show the flow of data through the modeling system.



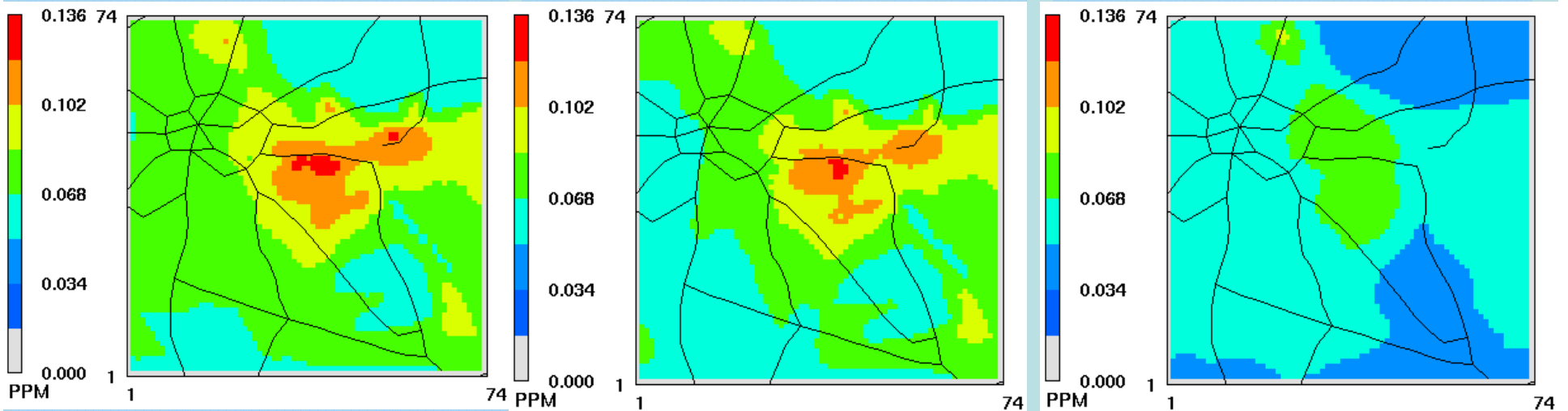
# Mobile Reductions – 2007 Control Case – Aug 31



**0% Reduction – 136 ppb**

**25% Reduction – 133 ppb**

**50% Reduction – 131 ppb**



**75% Reduction - 129**

**100 % Reduction – 127 ppb**

**0% mob, 0% pt – 88 ppb**

**1 km**