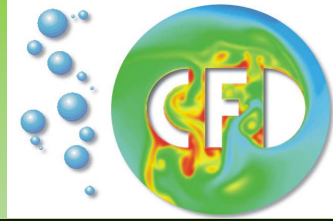




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A numerical set-up for benchmarking and optimization of fluid-structure interaction

Stefan Turek, Mudassar Razzaq and Jaroslav Hron
TU Dortmund, Germany

with support by M.Schäfer, M. Heck, M. Krafczyk, J. Tölke, S. Geller, H.-J. Bungartz, M. Brenk, R. Rannacher, T. Dunne, W. Wall, A. Gerstenberger, E. Rank, A. Düster, S. Kollmannsberger, K.-U. Bletzinger, R. Wüchner, A.Kupzok, T. Gallinger, U. Israel

Open Industrial Day Jyväskylä, Finland

March 16, 2009

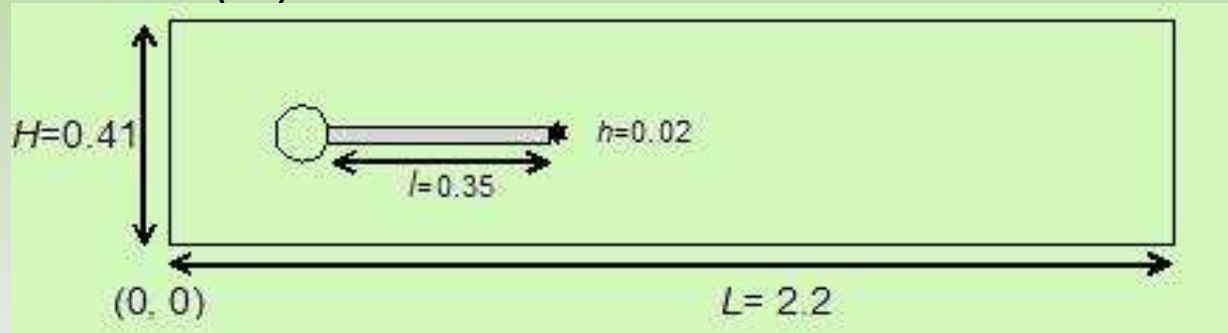
Integrated Multiphysics Simulations & Design optimization

Requirements for numerical FSI benchmarking

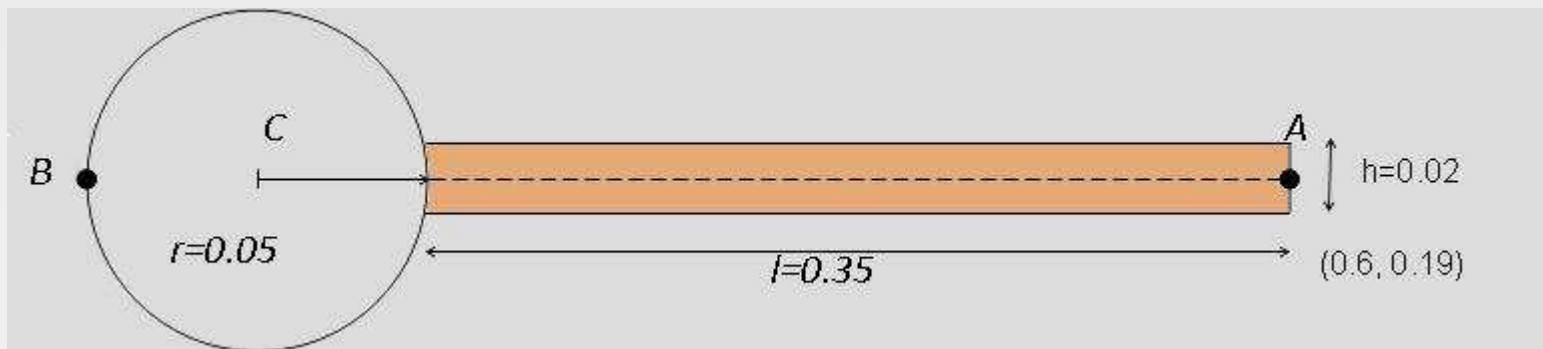
- *Realistic materials*
 - **incompressible Newtonian fluid**, laminar flow regime
 - **elastic solid**, large deformations
- *Comparative evaluation*
 - setup with periodical oscillations
 - non-graphically based quantities
- *Computable configurations*
 - laminar flow
 - reasonable aspect ratios
 - simple geometry (2D)
- Mainly based on validated CFD benchmarks, but also close to experimental set-up

Computational domain

- Domain dimensions (m)

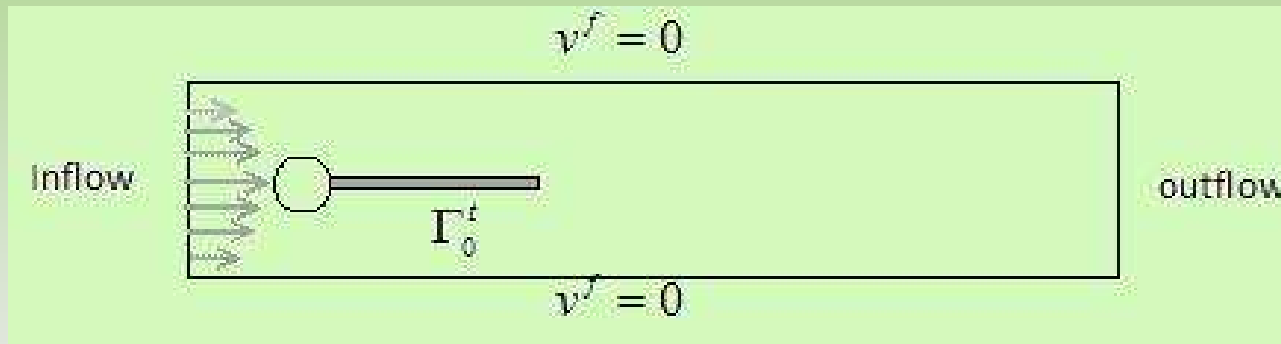


- Detail of the submerged structure



$$A(t=0) = (0.6, 0.2), \quad B = (0.15, 0.2), \quad C = (0.2, 0.2)$$

Boundary and initial conditions



- Inflow** parabolic velocity profile is prescribed at the left end of the channel
- Outflow** condition can be chosen by the user, assuming zero reference pressure

Otherwise the *no-slip* condition is prescribed for the fluid on the other boundary parts.

Initial no flow fluid and no deformation + smooth increase of the inflow profile

Fluid and structure properties

- **Incompressible** fluid with density ρ^f

$$\rho^f \frac{\partial \mathbf{v}^f}{\partial t} + \rho^f (\nabla \mathbf{v}^f) \mathbf{v}^f = \text{div } \boldsymbol{\sigma}^f \quad \text{in } \Omega_t^f$$
$$\text{div } \mathbf{v}^f = 0$$

$$\boldsymbol{\sigma}^f = -p^f \mathbf{I} + \rho^f \nu^f (\nabla \mathbf{v}^f + \nabla \mathbf{v}^{fT})$$

- Elastic material with density, ρ^s , $\mathbf{F} = \mathbf{I} + \nabla \mathbf{u}^s$, $J = \det \mathbf{F}$: **St. Venant -- Kirchhoff** material

$$\rho^s \frac{\partial^2 \mathbf{u}^s}{\partial t^2} = \text{div}(\boldsymbol{\sigma}^s \mathbf{F}^{-T}) \quad \text{in } \Omega^s$$

$$\boldsymbol{\sigma}^s = \frac{1}{J} \mathbf{F} (\lambda^s (\text{tr} \mathbf{E}) \mathbf{I} + 2\mu^s \mathbf{E}) \mathbf{F}^T$$

$$\mathbf{E} = \frac{1}{2} (\mathbf{F}^T \mathbf{F} - \mathbf{I})$$

Suggested material parameters

solid

- ρ^s density
- ν^s Poisson ratio
- μ^s shear modulus

fluid

- ρ^f density
- ν^f kinematic viscosity

Parameter	polybutadiene & glycerine	polypropylene & glycerine
$\rho^s [10^3 \text{ kg/m}^3]$	0.91	1.1
ν^s	0.50	0.42
$\mu^s [10^6 \text{ kg/ms}^2]$	0.53	317
$\rho^f [10^3 \text{ kg/m}^3]$	1.26	1.26
$\nu^f [10^{-3} \text{ m}^2 / \text{s}]$	1.13	1.13

Parameter	FSI1	FSI2	FSI3
$\rho^s [10^3 \text{ kg/m}^3]$	1	1	1
ν^s	0.4	0.4	0.4
$\mu^s [10^6 \text{ kg/ms}^2]$	0.5	0.5	2.0
$\rho^f [10^3 \text{ kg/m}^3]$	1	1	1
$\nu^f [10^{-3} \text{ m}^2 / \text{s}]$	1	1	1
$\bar{U} [\text{m/s}]$	0.2	1	2

Parameter	FSI1	FSI2	FSI3
$\beta = \frac{\rho^s}{\rho^f}$	1	1	1
ν^s	0.4	0.4	0.4
$Ae = \frac{E^s}{\rho^f \bar{U}^2}$	3.5×10^4	1.4×10^3	1.4×10^3
$Re = \frac{\bar{U} d}{\nu^f}$	20	100	200
$\bar{U} [\text{m/s}]$	0.2	1	2

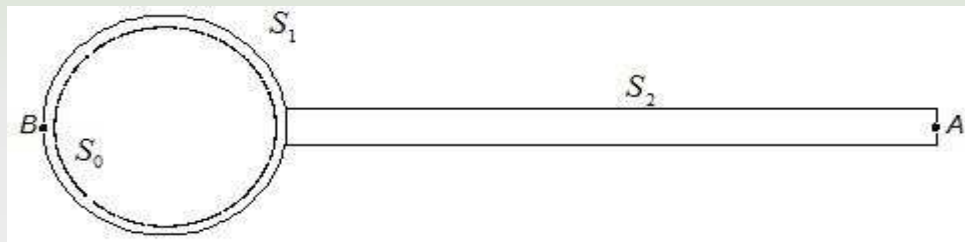
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Quantities of interest

- The position $A(t) = (x(t), y(t))$ of the end of the structure
- Pressure difference between the points $A(t)$ and B

$$\Delta p^{AB}(t) = p^B(t) - p^{A(t)}(t)$$

- Forces exerted by the fluid on the *whole body*, i.e. lift and drag forces acting on the cylinder and the structure together



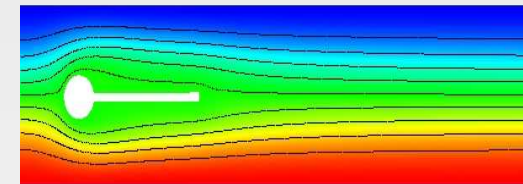
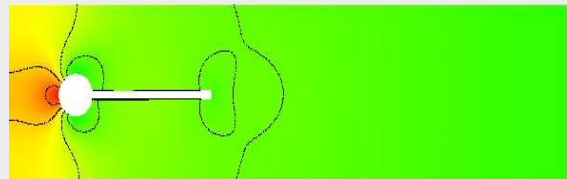
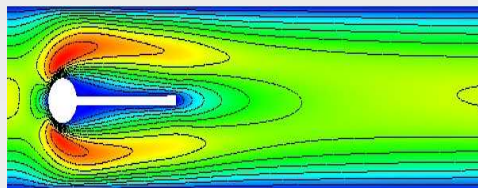
$$(F_D, F_L) = \int_S \sigma \, ndS = \int_{S_1} \sigma^f \, ndS + \int_{S_2} \sigma^{f|S} \, ndS = \int_{S_0} \sigma \, ndS$$

- Frequency and maximum amplitude
- Compare results for *one* full period and 3 different levels of spatial discretization h and 3 time step sizes Δt

FSI1: steady, small deformations

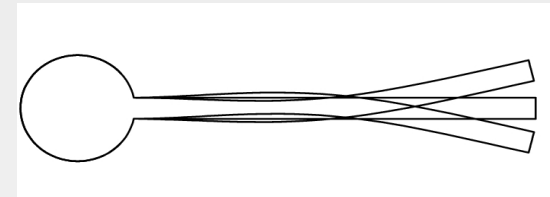
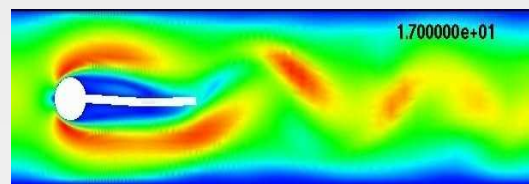
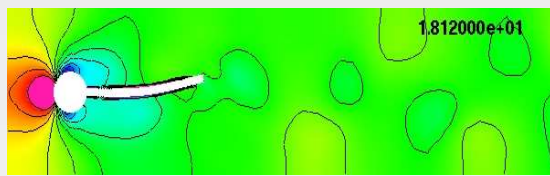
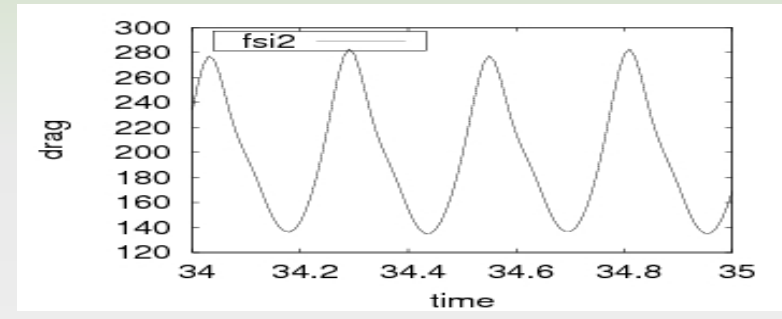
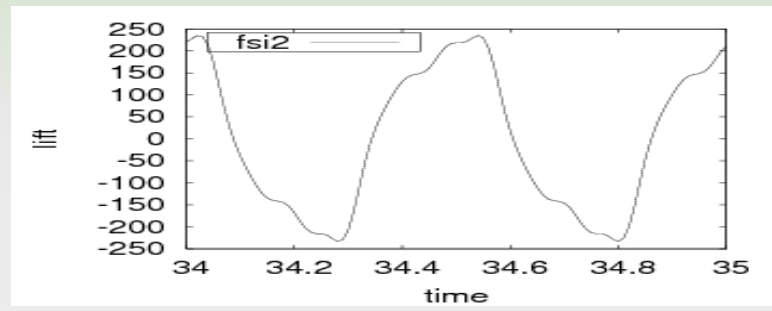
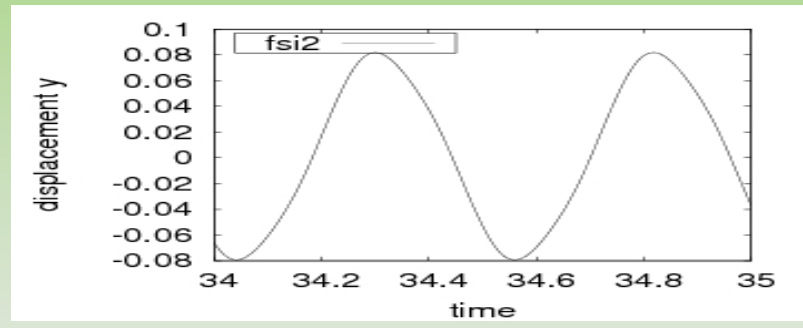
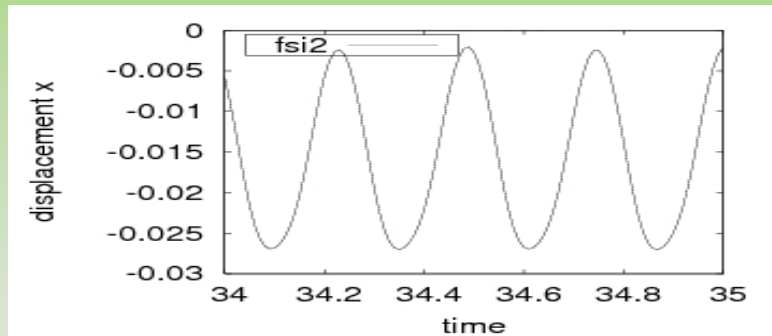
Parameter	FSI1	FSI2	FSI3
$\rho^s [10^3 \text{ kg/m}^3]$	1	1	1
ν^s	0.4	0.4	0.4
$\mu^s [10^6 \text{ kg/ms}^2]$	0.5	0.5	2.0
$\rho^f [10^3 \text{ kg/m}^3]$	1	1	1
$\nu^f [10^{-3} \text{ m}^2/\text{s}]$	1	1	1
$\bar{U} [\text{m/s}]$	0.2	1	2

Parameter	FSI1	FSI2	FSI3
$\beta = \frac{\rho^s}{\rho^f}$	1	1	1
$\nu^s \rho^f$	0.4	0.4	0.4
$Ae = \frac{E^s}{\rho^f \bar{U}^2}$	3.5×10^4	1.4×10^3	1.4×10^3
$Re = \frac{\bar{U} d}{\nu^f}$	20	100	200
$\bar{U} [\text{m/s}] \frac{\nu^f}{d}$	0.2	1	2



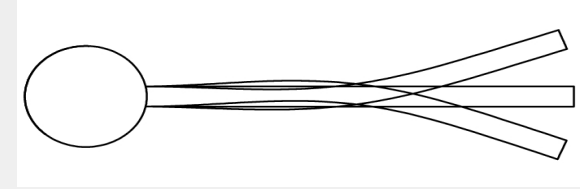
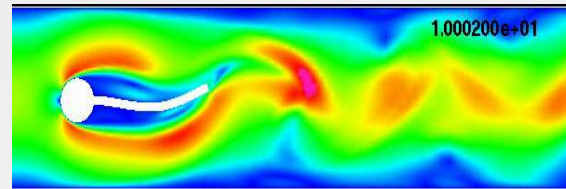
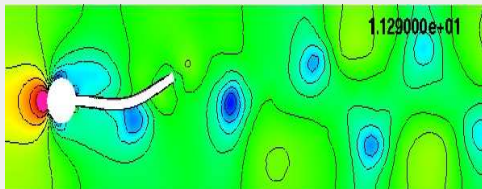
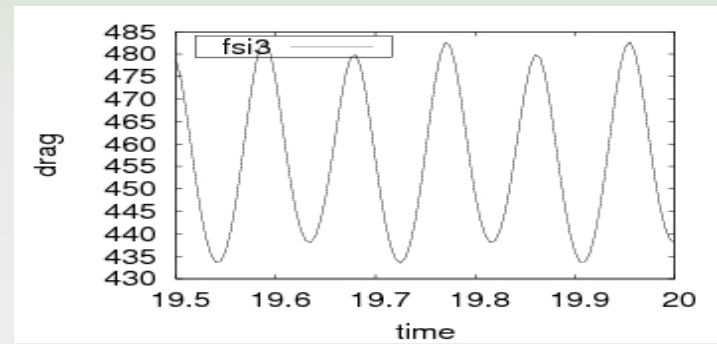
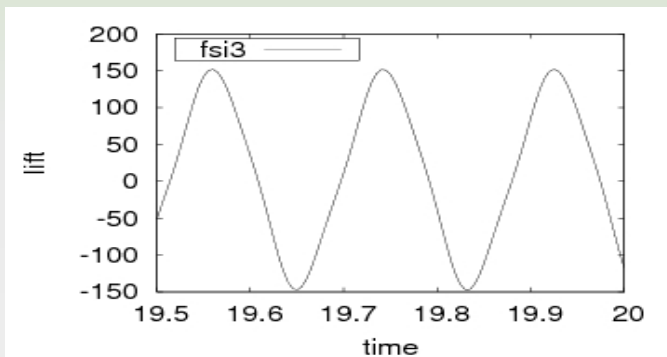
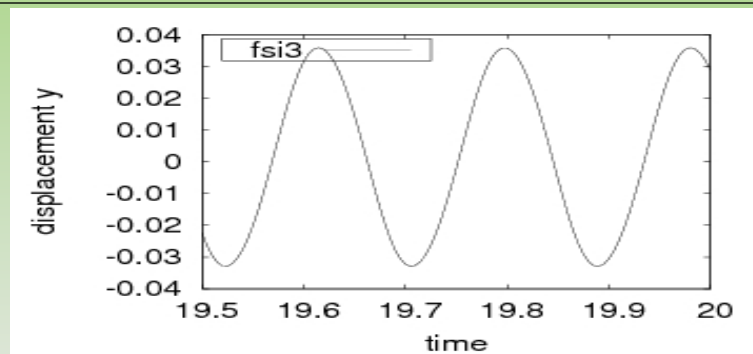
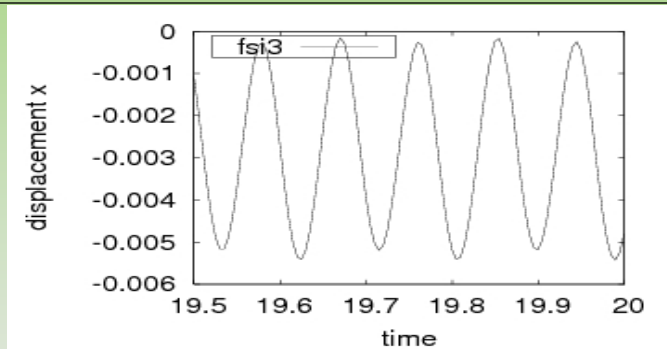
	ux of A [$\times 10^{-3}$ m]	uy of A [$\times 10^{-3}$ m]	drag	lift
FSI1	0.0227	0.8209	14.295	0.7638

FSI2: large deformations, periodical oscillations



Test	u_x of A $\times 10^{-3}$ m	u_y of A $\times 10^{-3}$ m	drag	lift
FSI2	$-14.58 \pm 12.44[3.8]$	$1.23 \pm 80.6[2.0]$	$208.83 \pm 73.75[3.8]$	$0.88 \pm 234.2[2.0]$

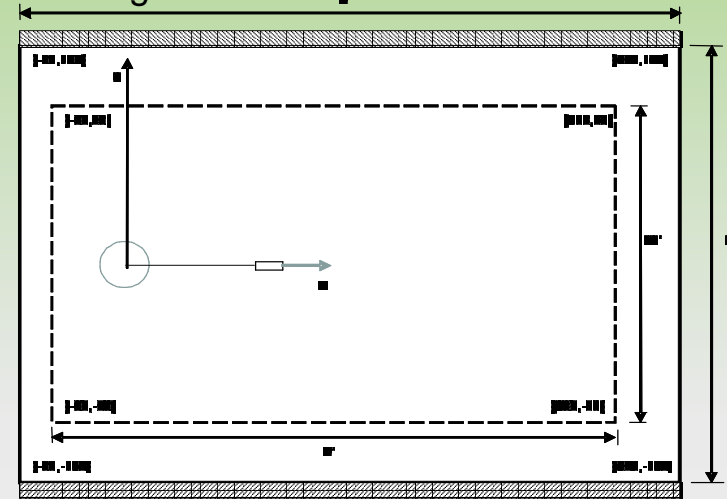
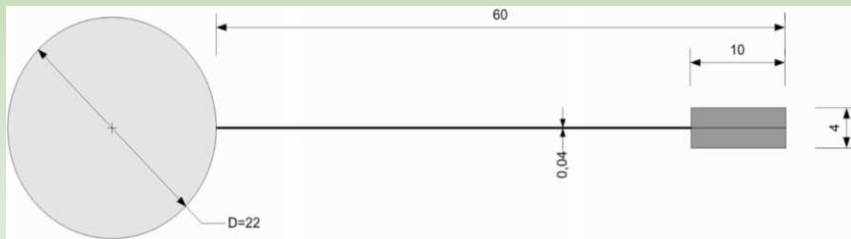
FSI3: large deformations, complex oscillations



Test	ux of A [$\times 10^{-3}$ m]	ux of A [$\times 10^{-3}$ m]	drag	lift
FSI3	$-2.69 \pm 2.53[10.9]$	$1.48 \pm 34.38[5.3]$	$457.3 \pm 22.66[10.9]$	$2.22 \pm 149.78[5.3]$

FSI4: Benchmarking of experimental data

- Flustruc experiment, Erlangen, <http://www.lstm.uni-erlangen.de/flustruc/>



fluid parameters	
density of the fluid	1.05e-6 [kg/mm ³]
kinematic viscosity	164.0

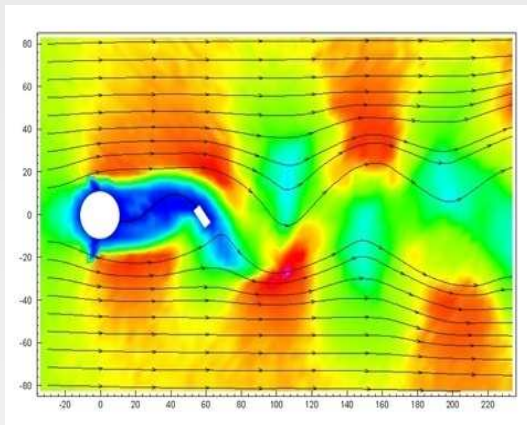
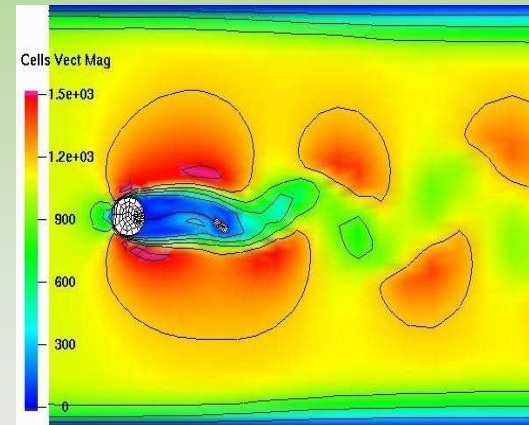
solid parameters	
density of the beam (steel)	7.85e-6[kg/mm ³]
density of the rear mass	7.8e-6 [kg/mm ³]
shear modulus	7.58e13
poisson ratio	0.3

geometry parameter		value [mm]
channel length	L	338.0
channel width	W	240.0
cylinder center position	C	(0.0, 0.0)
cylinder radius	R	11.0
elastic structure length	l	50
elastic structure thickness	w	0.04
rear mass length	w'	10.0
rear mass thickness	h'	4.0
reference point (at t=0)	A	(71.0, 0.0)
reference point	B	(11.0, 0.0)

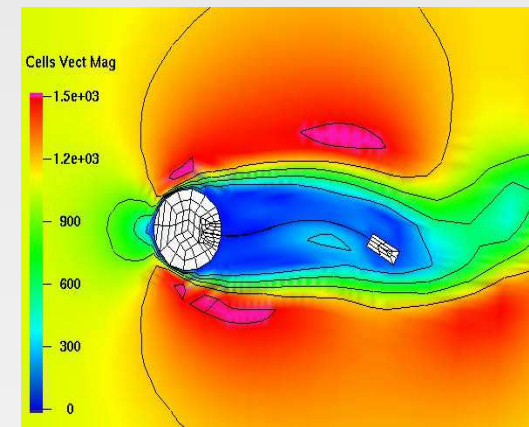
A numerical set-up for benchmarking and optimization of fluid-structure interaction

FSI4: New configuration

- + Laminar Flow (glycerine)
- + “2D“ flow and deformation
- Rotational degree of freedom
- Large aspect ratio (thin structure),
- Corners



Flustruc experiment, Erlangen



Computation

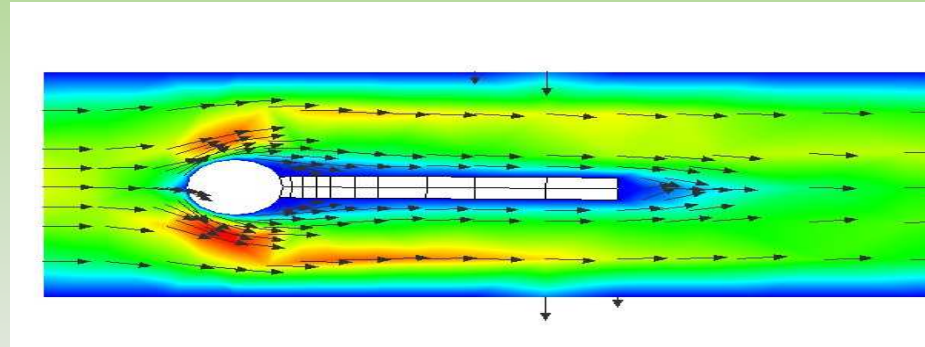
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FSI Optimization

- Optimization problem
 - Associated design or control variable
- The main design aims could be
 - I) Drag/Lift minimization
 - II) Minimal pressure loss
 - III) Minimal nonstationary oscillations
- To reach these aims, we might allow
 1. Boundary control of inflow section
 2. Change of geometry: elastic channel walls or length/thickness of elastic beam
 3. Optimal control of volume forces
- Optimal control of nonstationary flow might be hard for the starting
- Results for the moment are combination of I)-III) with 1)-3).

FSI Optimization: Example 1

- uncontrolled flow



	ux of A [$\times 10^{-3}$ m]	uy of A [$\times 10^{-3}$ m]	drag	lift
FSI1	0.0227	0.8209	14.295	0.7638

lift \neq 0

- Aim: minimize($lift^2 + \alpha V^2$)

w.r.t V1, V2.

V1 velocity from top

V2 velocity from below

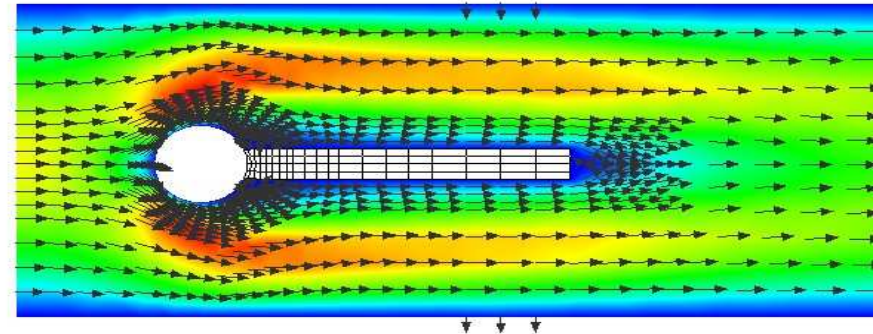
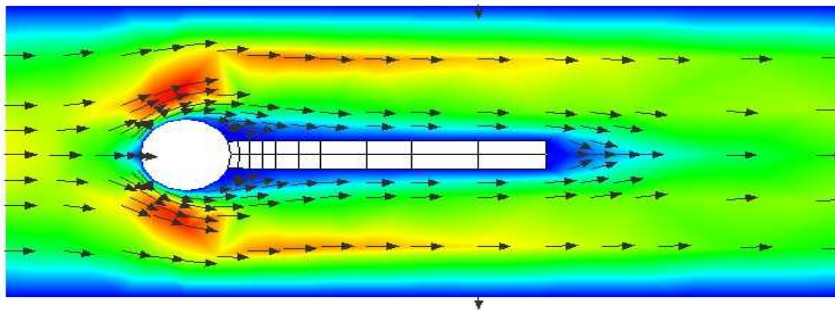
FSI Optimization: Example 1

➤ TESTS for FSI 1 (Boundary control)

level 1

level 2

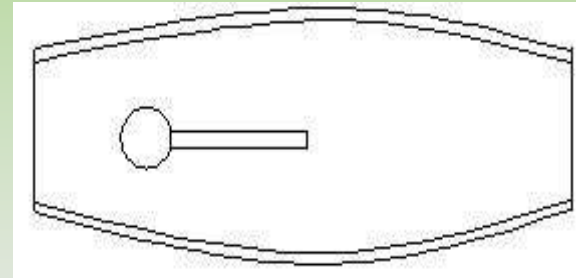
α	Iter steps	extreme point	drag	Lift	Iter steps	extreme point	drag	Lift
1e0	57	(3.74e-1,3.88e-1)	1.5471e+01	8.1904e-1	59	(3.66e-1,3.79e-1)	1.5550e+01	7.8497e-1
1e-2	60	(1.04e0,1.06e0)	1.5474e+01	2.2684e-2	59	(1.02e0,1.04e0)	1.5553e+01	2.1755e-2
1e-4	73	(1.06e0,1.08e0)	1.5474e+01	2.3092e-4	71	(1.04e0,1.05e0)	1.5553e+01	2.2147e-4
1e-6	81	(1.06e0,1.08e0)	1.5474e+01	2.3096e-6	86	(1.04e0,1.05e0)	1.5553e+01	2.2151e-6



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More examples

➤ further examples might be:




1. minimize($lift^2 + \alpha V^2$) for deformed case
2. pressure loss minimize: minimize($p_{in} - p_{out}$)
w.r.t elastic deformation of the wall
or
w.r.t geometrical and material properties of beam

Suggestions

0) Validate your FSI Code

1) FSI1 + EX1

send us results  until summer

1) Preliminary tests:

for other examples  discuss via internet, until fall